Petrology Spring 2006

Problem Set #4: Geothermal gradients

The expressions below can be used to calculate a conductive geothermal gradient for the lithosphere.

$$T(z) = Qz/K + A_0 z(b - z/2)/K + T_s$$
 $z < b$

$$T(z) = Qz/K + A_0b^2/(2K) + T_s$$
 $b \le z \le L$ where L=100 km

typical values

where: $T_s = \text{surface temperature (°C)}$ 15 $Q = \text{mantle heat flow (mW/m}^2)$ 30 K = thermal conductivity (W/m/deg) 2.5 $A_o = \rho H_s = \text{heat production } (\mu \text{W/m}^3)$ 2.0 $b = \text{characteristic depth of } A_o \text{ (km)}$ 10

z = depth (km)

Using a spreadsheet (e.g., Excel), plot temperature (°C) vs. depth (km) for

- a) the entire lithosphere (100 km), and
- b) the upper 35 km. Plot depth as the y-axis and "negative" (i.e., going down the page from 0 km).

Answer the following questions:

- 1. What is the temperature at the base of the lithosphere? _____ at 35 km? _____.
- 2. Play around with some of the parameters. What do you need to do to get 700°C at 35 km? Is there a unique solution? Which parameters do you think we know best? the least?

3. The equations given above assume that heat flow in the lithosphere is by conduction only. Is this a reasonable assumption? Why or why not?